

LIST 3. Extremes of Multivariable Functions.

Task 1: Find all extremes of the two variables functions:

$$a. f(x,y) = x^2 + y^2 - 3;$$

$$f. f(x,y) = x^2 + xy + y^2 - 4\ln x - 10\ln y,$$

$$b. f(x,y) = x^2 + xy + y^2 - 6x - 9y;$$

$$g. f(x,y) = x^3 y^2 (6-x-y) \quad (x>0 \ y>0),$$

$$c. f(x,y) = x^4 + 4xy + y^4 - 2x^2 - 2y^2;$$

$$h. f(x,y) = e^{2x+3y} (8x^2 - 6xy + 3y^2);$$

$$d. f(x,y) = x^2 y - xy^2 + \frac{y^3}{3} - 9y;$$

$$i. f(x,y) = (x^2 + y) \sqrt{e^y};$$

$$e. f(x,y) = 2xy - \frac{4}{x} - \frac{12}{y} \quad (x \neq 0 \ y \neq 0);$$

$$j. f(x,y) = (2x^2 + y^2) e^{-(x^2+y^2)}.$$

Task 2: Find all extremes of the three variables functions:

$$a. f(x,y,z) = x^2 + y^2 + z^2 - xy + x - 2z;$$

$$b. f(x,y,z) = x + \frac{y^2}{4x} + \frac{z^2}{y} + \frac{2}{z} \quad (x>0, \ y>0, \ z>0).$$