

LIST 5. Improper Integrals.

Task 1: Calculate improper integrals type 1 (if they are convergent):

$$\begin{array}{lll} a) \int_1^{+\infty} \frac{dx}{x^2(x+1)}; & b) \int_{-\infty}^{+\infty} \frac{dx}{3x^2 + 12x + 24}; & c) \int_0^{+\infty} \frac{dx}{x^3 + 1}; \\ d) \int_1^{+\infty} \frac{\arctan x}{x^2} dx; & e) \int_0^{+\infty} e^{-x} \sin x dx; & f) \int_0^{+\infty} x \sin x dx. \end{array}$$

Task 2: Calculate improper integrals type 2 (if they are convergent):

$$\begin{array}{lll} a) \int_0^1 x \ln x dx; & b) \int_1^e \frac{dx}{x \ln x}; & c) \int_1^2 \frac{dx}{\sqrt{x-1}}; \\ d) \int_1^e \frac{dx}{\sin x}; & e) \int_1^2 \frac{dx}{\sqrt{(x-1)(2-x)}}; & f) \int_0^2 \frac{dx}{\sqrt[3]{(x-1)^2}}. \end{array}$$

Task 3: Calculate area of the surface limited by axes of coordinate system and the graph of the function $y = e^{-2x}$, for $x > 0$

Task 4: Calculate the volume of solid of revolution formed by rotation of graph of the function below (around the x-axis):

$$y = \frac{1}{x}, \text{ for } x \geq 1.$$