

LIST 1.
Differential equations 1st order.

Task 1: Solve the equations by separating the variables:

a) $y' - xy^2 = 2xy$; b) $y' = \sqrt{y}e^{3x}$; c) $(1 + x^2)y' = 2xy$;
d) $\sin y' = x$; e) $y' \operatorname{tg} x - y = -2$; f) $y' + (1 - y^2) \operatorname{tg} x = 0$.

Task 2: Solve the equations by a separating the variables using substitutions:

a) $y' = \cos(y - x)$; b) $y' - y = 2x - 3$; c) $y' = \sqrt{4x + 2y - 1}$.

Task 3: Find a solution of equations with separated variables satisfying the initial conditions:

a) $yy' + 4x = 0$, $y(0) = 4$; b) $dy = 2xy^2 dx$, $y(0) = 1$; c) $x(y^2 - 1)dx + y(x^2 - 1)dy = 0$, $y(0) = 2$.

Task 4: Solve linear differential equations:

a) $xy' - 2y = 2x^4$; b) $x(y' - y) = e^x$; c) $y = x(y' - x \cos x)$; d) $y' = \frac{y}{3x - y^2}$;
e) $xy' + (x + 1)y = 3x^2 e^{-x}$; f) $(2x + 1)y' = 4x + 2y$; g) $y' = 2x(x^2 + y)$.

Task 5: Find a solution of linear differential equations with satisfying the initial conditions:

a) $y' + \frac{3}{x}y = \frac{2}{x^3}$, $y(1) = 1$; b) $xy' = x - y$, $y(0) = 0$.
c) $y' - 2xy = 1$, $y(0) = 0$; d) $xy' = x + 2y$, $y(0) = 0$